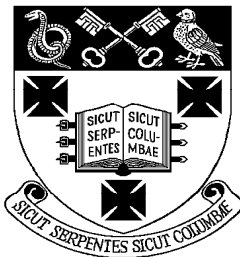


RADLEY COLLEGE
Entrance Scholarships



MATHEMATICS I

Thursday 13th February 2003

Time allowed 90 minutes

*You may try the questions in any order and
are not expected to complete them all.*

Show all working.

1. (No calculating aids are to be used in this question)

a) Work out exactly

i) 60.8×2.71

ii) $172.02 \div 47$

b) Give the answers to the following as fractions in their simplest form

i) $\frac{13}{15} - \frac{7}{10}$

ii) $7\frac{1}{2} \div 5\frac{1}{4}$

iii) $\left(7\frac{2}{3} + 1\frac{4}{5}\right) \times 1\frac{5}{22}$

c) Give the answers to the following in standard form.

i) $(7 \times 10^6) + (5 \times 10^6)$

ii) $(6 \times 10^3) \times (4 \times 10^{-4})$

iii) $(4.8 \times 10^2) \div (6 \times 10^5)$

2. (No calculating aids are to be used in this question)

Work out as simply as possible

a) $923^2 - 77^2$

b) $38^2 + (93 \times 38) - (38 \times 31)$

c) $(83 \times 47) + (17 \times 24) + (36 \times 83) - (41 \times 17)$

d) $\frac{456^2 + (456 \times 44)}{45.6 \times 25}$

3. a) Multiply out and simplify

i) $(2x + y)^2$

ii) $(3x + y)(9x^2 - 3xy + y^2)$

b) Factorise fully

i) $12x^2y + 16xy^2$

ii) $27 - 12x^2$

iii) $x^2 - 11x + 18$

c) Simplify

i) $\frac{xy + xz}{y^2 - z^2}$

ii) $\frac{x^2}{y^3} \div x^2y^2$

4. Solve each of these equations for x

a)
$$\frac{3x+1}{2} + \frac{2x+1}{7} = 6$$

b)
$$2x^2 - 6x = 0$$

c)
$$\frac{42}{x+2} + 6 = \frac{78}{x+2}$$

d)
$$(3x+1)(x+2) - 3x^2 = 37$$

5. Rearrange each of the following formulae to make x the subject

a)
$$a = bx - c$$

b)
$$\frac{a}{x+b} = \frac{c}{x+d}$$

c)
$$\sqrt{x-a} = b$$

6. In cricket a batsman's average is calculated by dividing the total number of runs he has scored by the number of times he is out. So a batsman who has played 11 innings scoring a total of 400 runs and has been not out three times has an average of 50. ($400 \div (11 - 3) = 50$).

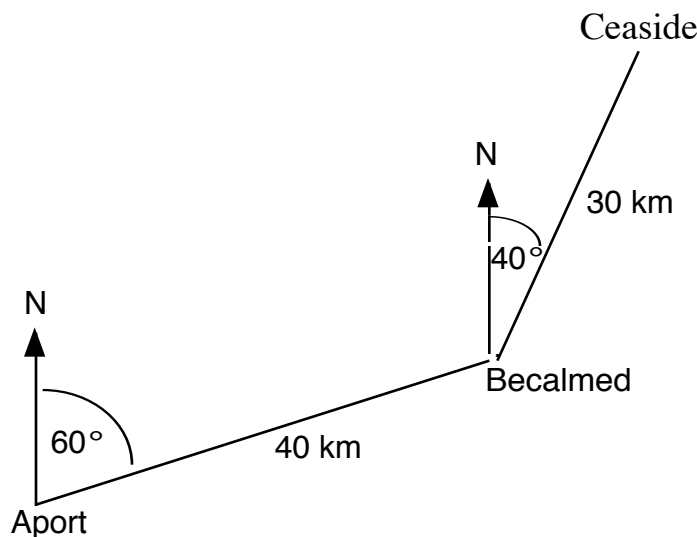
Matthew Matics has become a keen cricketer. In the last match of the season, he scored 63 runs before he was out. He works out that this improved his season's average by 5. Letting x be the total he had scored before the final match and letting y be the number of times he had been out previously, write down an equation in x and y and show that it simplifies to $x + 5y^2 - 58y = 0$.

Then he realises that had he not been out (but still have scored 63 runs), his season's average would have been improved by 9 in the last match. Write down and simplify an equation using this piece of information.

Find the values of x and y , and thus find Matthew's batting average for the season.



7. A yachtsman sails 40 km on a bearing 060° from Aport to Becalmed, and then changes direction to sail 30 km on 040° to get to Ceaside.



- How far East of Aport is Becalmed?
 - How far North of Aport is Becalmed?
 - How far East of Aport is Ceaside?
 - How far North of Aport is Ceaside?
 - Had the yachtsman wanted to sail directly from Aport to Ceaside, how far would it have been and on what bearing?
8. For any positive integer, n , we define $n!$ to be the product of all the integers between 1 and n inclusive.

So, for example, $5! = 1 \times 2 \times 3 \times 4 \times 5 = 120$

- (a) Work out
- $3!$
 - $6!$
 - $1!$

(b) For two positive integers, a and b , where $a > b$, we define an operation $*$ such that $a * b = \frac{a!}{(a-b)!}$

(i) Show that $6 * 2 = 30$

(ii) Work out $7 * 3$.

(c) Show that $n * 1 = n$, and work out a similar expression for $n * 2$.

(d) Solve the equation $n * 2 = 8n -$